Please check the examination details bel	ow before entering your candidate information		
Candidate surname	Other names		
Pearson Edexcel Inter			
Thursday 8 June 2023			
Morning (Time: 2 hours)	Paper reference 4PM1/02		
Further Pure Mat	hematics		
Calculators may be used.	Total Marks		

# **Instructions**

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- You must NOT write anything on the formulae page.
   Anything you write on the formulae page will gain NO credit.

# Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

### **Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶





## **International GCSE in Further Pure Mathematics Formulae sheet**

### Mensuration

**Surface area of sphere** =  $4\pi r^2$ 

**Curved surface area of cone** =  $\pi r \times \text{slant height}$ 

Volume of sphere =  $\frac{4}{3}\pi r^3$ 

### Series

### **Arithmetic series**

Sum to *n* terms,  $S_n = \frac{n}{2} [2a + (n-1)d]$ 

### Geometric series

Sum to *n* terms, 
$$S_n = \frac{a(1-r^n)}{(1-r)}$$

Sum to infinity,  $S_{\infty} = \frac{a}{1-r} |r| < 1$ 

### **Binomial series**

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$$
 for  $|x| < 1, n \in \mathbb{Q}$ 

### **Calculus**

### **Quotient rule (differentiation)**

$$\frac{\mathrm{d}}{\mathrm{d}x} \left( \frac{\mathrm{f}(x)}{\mathrm{g}(x)} \right) = \frac{\mathrm{f}'(x)\mathrm{g}(x) - \mathrm{f}(x)\mathrm{g}'(x)}{\left[\mathrm{g}(x)\right]^2}$$

### **Trigonometry**

### Cosine rule

In triangle ABC:  $a^2 = b^2 + c^2 - 2bc \cos A$ 

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

### Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$



# Answer all ELEVEN questions.

# Write your answers in the spaces provided.

# You must write down all the stages in your working.

1 Given that  $\frac{a+2\sqrt{5}}{3-\sqrt{5}} = \frac{11+b\sqrt{5}}{2}$  where a is an integer and b is prime,

find the value of a and the value of b Show your working clearly.

(5)



(Total for Question 1 is 5 marks)

2	The <i>n</i> th term of a convergent geometric series is $8^{(1-2n)}$					
	Find the sum to infinity of the series.					
	Give your answer in the form $\frac{p}{q}$ where p and q are integers to be found.					
		(6)				





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Figure 1

Figure 1 shows a circle, centre O, with radius rcm.

The points A, P and B lie on the circle.

The obtuse angle  $AOB = \theta$  radians.

The area of the sector APBO, shown shaded, is  $372.4 \,\mathrm{cm^2}$  and the length of the arc APB is  $53.2 \,\mathrm{cm}$ .

Find, to 3 significant figures where appropriate, the value of

- (i) *r*
- (ii)  $\theta$



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B

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Figure 2

The curve S with equation  $y = \frac{x^2}{4} + 2$  where  $x \ge 0$  and the line l with equation 2y - x - 4 = 0 where  $x \ge 0$  intersect at the points A and B, as shown in Figure 2.

(a) (i) Show that the coordinates of point A are (0, 2)

0

(ii) Find the coordinates of the point B

(4)

The finite region bounded by S and l, shown shaded in Figure 2, is rotated through  $2\pi$  radians about the y-axis.

(b) Use algebraic integration to find the volume of the solid generated. Give your answer in terms of  $\pi$ 

(4)



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Question 4 continued		



- 5 (a) On the grid opposite draw the line with equation
  - (i) y = 2x + 5
- (ii) 4y = x 8
- (iii) 5y + 3x = 30

(3)

(b) Show, by shading, the region R defined by the inequalities

$$y \leqslant 2x + 5$$

$$4y \geqslant x - 8$$

$$5y + 3x \leq 30$$

(1)

For all points in R with coordinates (x, y)

$$P = 2x - 5y$$

(c) Using your graph, find the least value of P

(3)

# **Question 5 continued** 9 8 $\Box O$ Turn over for a spare grid if you need to redraw your graph.



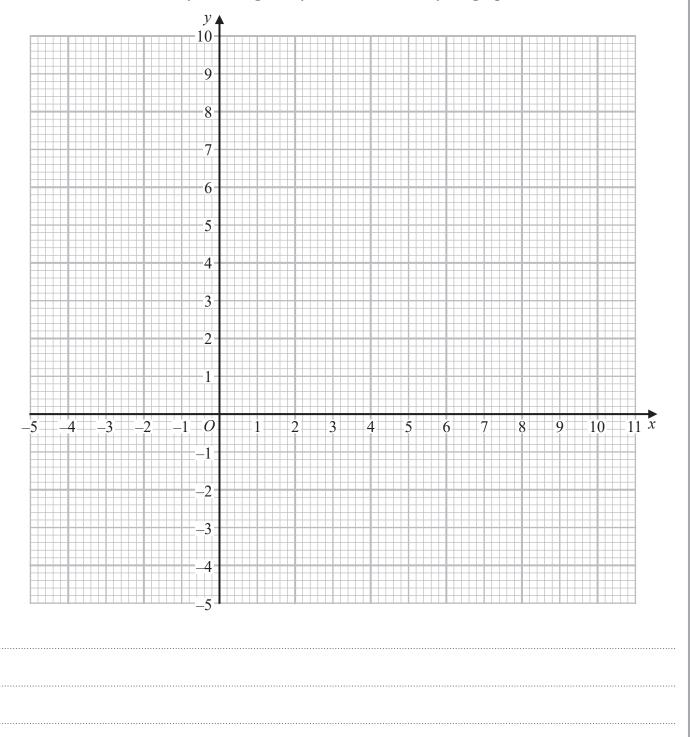
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Question 5 continued	



# **Question 5 continued**

Only use this grid if you need to redraw your graph.



(Total for Question 5 is 7 marks)



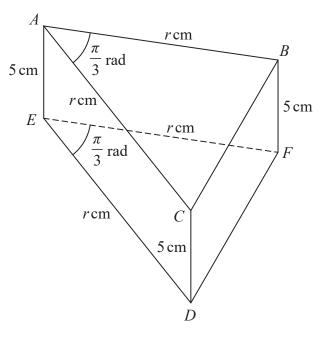


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Figure 3

Figure 3 shows a right triangular prism ABCDEF. A cross section ABC of the prism is a triangle in which AB = AC = r cm and  $\angle CAB = \frac{\pi}{3}$  radians.

In the prism

$$AE = BF = CD = 5 \text{ cm}$$
  $ED = EF = r \text{ cm}$  and  $\angle DEF = \frac{\pi}{3}$  radians

(a) Show that the volume of the prism is  $\frac{5\sqrt{3}}{4} r^2 \text{ cm}^3$ 

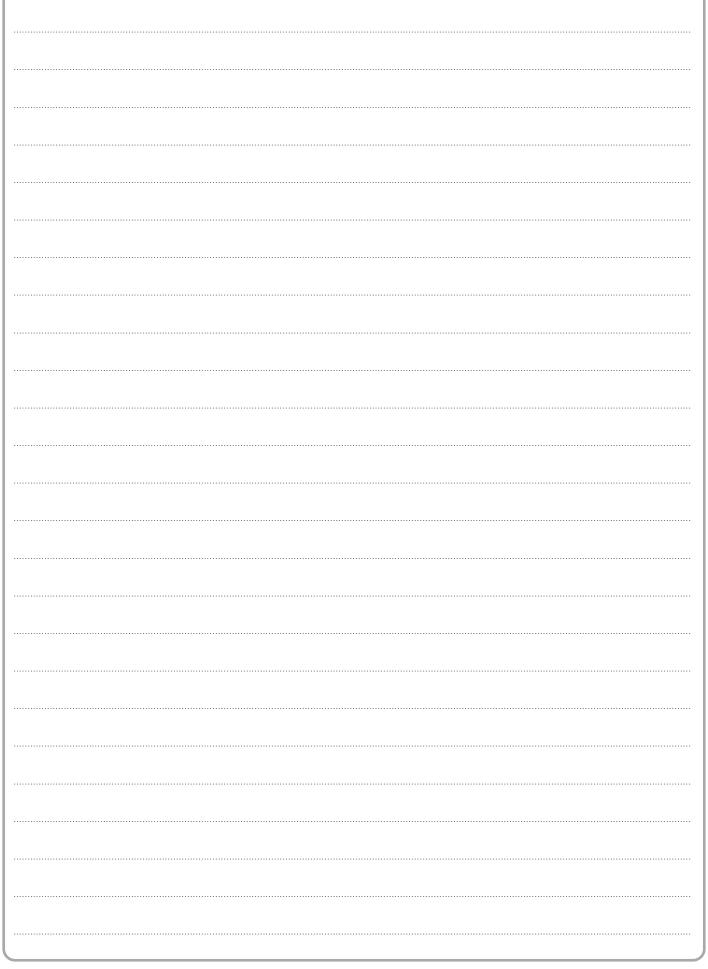
(1)

The volume of the prism is increasing in such a way that the size of  $\angle CAB$  and the size of  $\angle DEF$  remain constant and the length of AE, the length of BF and the length of CD remain constant.

The lengths of AB, AC, ED and EF are each increasing at a constant rate of 0.2 cm/s

(b) Find the exact rate of increase, in  $cm^3/s$ , of the volume of the prism when the area of the rectangular face BCDF is  $60\,cm^2$ 

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Question 6 continued



7 (a) Expand  $\left(1 + \frac{x}{3}\right)^{-3}$  in ascending powers of x up to and including the term in  $x^3$ 

Where appropriate express each coefficient as an exact fraction in its lowest terms.

(b) Write down the range of values of x for which your expression is valid.

(1)

(3)

(c) Express  $(3+x)^{-3}$  in the form  $P(1+Qx)^{-3}$  where P and Q are rational numbers whose values should be stated.

(2)

$$f(x) = \frac{(1+4x)}{(3+x)^3}$$

(d) Obtain a series expansion for f(x) in ascending powers of x up to and including the term in  $x^2$ 

(2)

(e) Hence, using algebraic integration, obtain an estimate of  $\int_0^{0.2} f(x) dx$  Give your answer to 5 significant figures.

(3)




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Question 7 continued





The points $A$ and $B$ have coordinates $(-6, 8)$ and $(12, 2)$ respectively.	
(a) Find an equation of the straight line passing through $A$ and $B$ in the form $ax + by + c = 0$ , where $a$ , $b$ and $c$ are integers to be found.	
	(3)
(b) Find the exact length of AB	(2)
	(2)
The point X with coordinates $(m, n)$ lies on AB such that $AX:XB = 1:2$	
(c) Find the value of m and the value of n	(2)
	(2)
The line L passes through the point X and is perpendicular to AB The point C with coordinates $(p, q)$ lies on L where $p > 0$ and $q > 0$	
Given that $AB$ is a diameter of a circle and $C$ also lies on the circumference of the circle	,
(d) find	
(i) the exact value of $p$	
(ii) the exact value of $q$	
	(7)
(e) Find the exact area of triangle ABC	
	(3)







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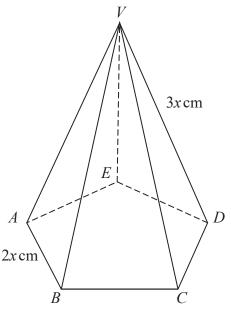


Diagram **NOT** accurately drawn

Figure 4

Figure 4 shows a right pyramid with vertex V and base ABCDE which is a regular pentagon.

$$AB = BC = CD = DE = EA = 2x \text{ cm}$$

$$VA = VB = VC = VD = VE = 3x \text{ cm}$$

Find, in degrees to one decimal place, the size of the angle between the plane VBC and the base ABCDE

(6)



- 10 The curve C with equation  $y = \frac{6-3x}{x-4}$  where  $x \neq 4$ , crosses the x-axis at the point P and the y-axis at the point Q
  - (a) Find the coordinates of
    - (i) *P*
- (ii) *Q*

**(2)** 

- (b) Write down an equation of the asymptote to C which is
  - (i) parallel to the *y*-axis
- (ii) parallel to the x-axis

**(2)** 

(c) Sketch C showing clearly the asymptotes and the coordinates of the points P and Q

(3)

The line *L* is the normal to *C* at the point on *C* where x = 2

(d) Find an equation of L

(6)

The line L intersects C again at the point R

(e) Find the x coordinate of R

(3)





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Question 10 continued





11 The roots of a quadratic equation E are  $\alpha$  and  $\beta$  where  $\alpha > \beta > 0$ 

Given that  $\alpha - \beta = 2\sqrt{6}$  and  $\alpha^2 + \beta^2 = 30$ 

- (a) show that
  - (i)  $\alpha\beta = 3$

**(4)** 

(ii)  $\alpha + \beta = 6$ 

**(2)** 

- (b) Without solving E
  - (i) find the value of  $\alpha^4 + \beta^4$

(2)

(ii) find the exact value of  $\alpha^4 - \beta^4$ 

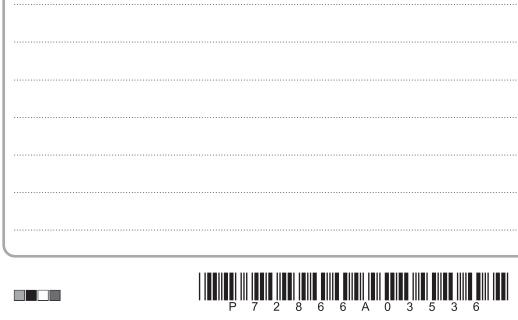
(2)

Given that  $\alpha^4 = P + Q\sqrt{6}$  where P and Q are positive integers,

(c) find the value of P and the value of Q

(2)





Question 11 continued	
	(Total for Question 11 is 12 marks)